

Errata to “Representations of finite groups of Lie type”, LMS Student texts no. 95

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Proposition 6.1.12 is wrong (thanks to Jay Taylor for noticing that). It should read

Proposition 6.1.12 *If (\mathbf{L}_I, Λ) is a cuspidal pair where Λ is a unipotent character (see Definition 11.3.4), then W_I is normalised by w_J for any F -stable $J \subset S$ containing I , where w_J is the longest element of the Coxeter group W_J ; $W_{\mathbf{G}^F}(\mathbf{L}_I)$ is a Coxeter group with generating simple reflections the elements $w_J w_I$ where $J \supset I$ and $J - I$ is a single orbit under F .*

The proof actually proves this corrected statement.

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The function $R_{(1,\varepsilon)}$ is equal to $\eta q^2 \mathcal{Y}_{(G_2(a_1),\varepsilon)}$ where $\eta = \pm 1$ is equal to $q \pmod{3}$. Consequently table 14.2 is wrong.

The values of unipotent characters of G_2 on unipotent classes ($p \neq 2, 3$):

	1	A_1	\tilde{A}_1	$G_2(a_1)_3$	$G_2(a_1)_2$	$G_2(a_1)$	G_2
1	1	1	1	1	1	1	1
St	q^6
σ	$\frac{q}{3}\Phi_3\Phi_6$	$-\frac{q}{3}\Phi_1\Phi_2$	q	$\frac{q}{3}(\eta q + 5)$	$-\frac{q}{3}(\eta q - 1)$	$\frac{q}{3}(\eta q - 1)$.
τ	$\frac{q}{3}\Phi_3\Phi_6$	$\frac{q}{3}(2q^2 + 1)$.	$\frac{q}{3}(\eta q - 1)$	$-\frac{q}{3}(\eta q - 1)$	$\frac{q}{3}(\eta q + 2)$.
ρ	$\frac{q}{6}\Phi_2^2\Phi_3$	$\frac{q}{6}(2q + 1)\Phi_2$	$\frac{q}{2}\Phi_2$	$\frac{q}{6}(\eta q + 5)$	$-\frac{q}{6}(\eta q - 1)$	$\frac{q}{6}(\eta q - 1)$.
ρ'	$\frac{q}{2}\Phi_2^2\Phi_6$	$\frac{q}{2}\Phi_2$	$\frac{q}{2}\Phi_2$	$-\frac{q}{2}(\eta q - 1)$	$\frac{q}{2}(\eta q + 1)$	$-\frac{q}{2}(\eta q - 1)$.
$\gamma_{[-1]}$	$\frac{q}{2}\Phi_1^2\Phi_3$	$-\frac{q}{2}\Phi_1$	$-\frac{q}{2}\Phi_1$	$-\frac{q}{2}(\eta q - 1)$	$\frac{q}{2}(\eta q + 1)$	$-\frac{q}{2}(\eta q - 1)$.
$\gamma_{[1]}$	$\frac{q}{6}q\Phi_1^2\Phi_6$	$\frac{q}{6}(2q - 1)\Phi_1$	$-\frac{q}{2}\Phi_1$	$\frac{q}{6}(\eta q + 5)$	$-\frac{q}{6}(\eta q - 1)$	$\frac{q}{6}(\eta q - 1)$.
$\gamma_{[\zeta_3]}$	$\frac{q}{3}\Phi_1^2\Phi_2^2$	$-\frac{q}{3}\Phi_1\Phi_2$.	$\frac{q}{3}(\eta q - 1)$	$-\frac{q}{3}(\eta q - 1)$	$\frac{q}{3}(\eta q + 2)$.
$\gamma_{[\zeta_3^2]}$	$\frac{q}{3}\Phi_1^2\Phi_2^2$	$-\frac{q}{3}\Phi_1\Phi_2$.	$\frac{q}{3}(\eta q - 1)$	$-\frac{q}{3}(\eta q - 1)$	$\frac{q}{3}(\eta q + 2)$.