The $\bar{\partial}$ -approach to approximate inverse scattering at fixed energy in three dimensions

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Abstract :

We develop the $\bar{\partial}$ -approach to inverse scattering at fixed energy in dimension $d \geq 3$ of [Beals,Coifman 1985] and [Henkin,Novikov 1987]. As a result we propose a stable method for nonlinear approximate finding a potential v from its scattering amplitude f at fixed energy E > 0 in dimension d = 3. In particular, in three dimensions we stably reconstruct n-times smooth potential v with sufficient decay at infinity, n > 3, from its scattering amplitude f at fixed energy up to $O(E^{-(n-3-\varepsilon)/2})$ in the uniform norm as $E \to +\infty$ for any fixed arbitrary small $\varepsilon > 0$ (that is with almost the same decay rate of the error for $E \to +\infty$ as in the linearized case near zero potential).

This talk is based, mainly, on [R.G.Novikov, International Mathematics Research Papers 2005 :6, 287-349 (2005)].