

# Séminaire de théorie des nombres

Le 26 mars 2007 à 15h30

## The modularity of Calabi–Yau threefolds over $\mathbf{Q}$

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**Résumé :** We will discuss the modularity of Galois representations associated to Calabi–Yau threefolds over  $\mathbf{Q}$ . We can show that any rigid Calabi–Yau threefold over  $\mathbf{Q}$  is modular i.e., its two-dimensional Galois representation comes from a modular form of weight 4 on some congruence subgroup of  $PSL_2(\mathbf{Z})$ . However, when a Calabi–Yau threefold is non-rigid, the dimension of the Galois representation gets rather large, and the modularity question poses a serious challenge. We will construct explicit examples of non-rigid Calabi–Yau threefolds fibered over  $\mathbf{P}^1$  by non-constant semi-stable  $K3$  surfaces and reaching the Arakelov–Yau upper bound. For these examples, we prove that the “interesting” part of their  $L$ -series do come from modular forms.