Séminaire de théorie des nombres

Le 18 décembre 2006 à 14h

J-invariant of an algebraic group

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Résumé : Let G be a linear algebraic group over a field F and X be a projective homogeneous G-variety such that G splits over the function field of X. We introduce an invariant of G called J-invariant which characterizes the splitting properties of the Chow motive of X. As a main application we obtain a uniform proof of all known motivic decompositions of generically split projective homogeneous varieties (Severi-Brauer varieties, Pfister quadrics, maximal orthogonal Grassmannians, G_2- and F_4-varieties) as well as provide new ones (exceptional varieties of types E_6, E_7 and E_8). We also discuss applications to torsion indices, canonical dimensions and splitting properies of the group G.