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Algebraic independence of periods of elliptic curves

Michel Waldschmidt

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Some of these paper are available on the internet. See in particular

http://www.imj-prg.fr/~michel.waldschmidt/texts.html

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